Solving simultaneous equations graphically

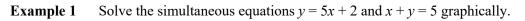
A LEVEL LINKS

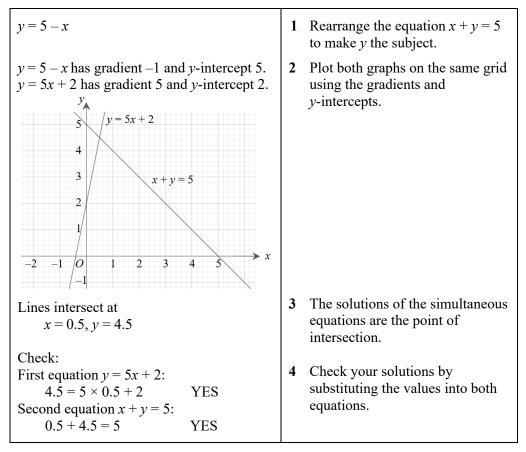
Scheme of work: 1c. Equations – quadratic/linear simultaneous

Key points

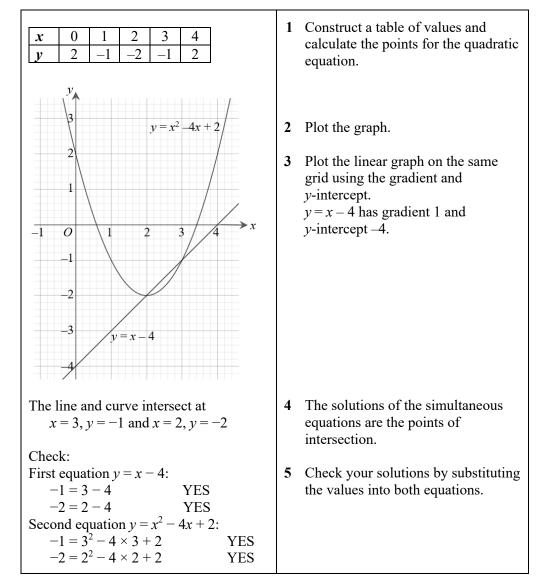
• You can solve any pair of simultaneous equations by drawing the graph of both equations and finding the point/points of intersection.

Examples









Example 2 Solve the simultaneous equations y = x - 4 and $y = x^2 - 4x + 2$ graphically.

Practice

- 1 Solve these pairs of simultaneous equations graphically.
 - **a** y = 3x 1 and y = x + 3
 - **b** y = x 5 and y = 7 5x
 - c y = 3x + 4 and y = 2 x

2 Solve these pairs of simultaneous equations graphically.

- **a** x + y = 0 and y = 2x + 6
- **b** 4x + 2y = 3 and y = 3x 1
- c 2x + y + 4 = 0 and 2y = 3x 1

Hint

Rearrange the equation to make *y* the subject.



- **3** Solve these pairs of simultaneous equations graphically.
 - **a** y = x 1 and $y = x^2 4x + 3$
 - **b** y = 1 3x and $y = x^2 3x 3$
 - c y = 3 x and $y = x^2 + 2x + 5$
- 4 Solve the simultaneous equations x + y = 1 and $x^2 + y^2 = 25$ graphically.

Extend

- 5 a Solve the simultaneous equations 2x + y = 3 and $x^2 + y = 4$
 - i graphically
 - ii algebraically to 2 decimal places.
 - **b** Which method gives the more accurate solutions? Explain your answer.



Answers

- 1 **a** x = 2, y = 5 **b** x = 2, y = -3**c** x = -0.5, y = 2.5
- **2 a** x = -2, y = 2**b** x = 0.5, y = 0.5
 - **c** x = -1, y = -2
- 3 **a** x = 1, y = 0 and x = 4, y = 3 **b** x = -2, y = 7 and x = 2, y = -5**c** x = -2, y = 5 and x = -1, y = 4
- 4 x = -3, y = 4 and x = 4, y = -3
- 5 a i x = 2.5, y = -2 and x = -0.5, y = 4ii x = 2.41, y = -1.83 and x = -0.41, y = 3.83
 - **b** Solving algebraically gives the more accurate solutions as the solutions from the graph are only estimates, based on the accuracy of your graph.

